

Particle Transport, Deposition and Removal Clarkson University

Particle Adhesion and Detachment Models

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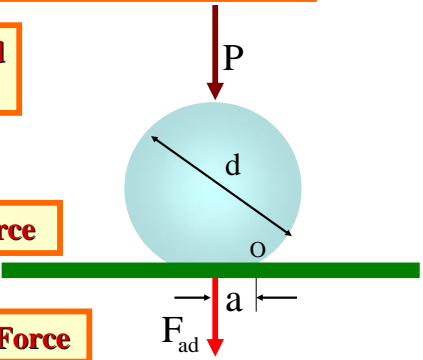
Outline Clarkson University

- Particle Detachment Mechanisms
- JKR Adhesion Model
- DMT Adhesion Model
- Maugis-Pollock Model
- Maximum Moment Resistance

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Particle Adhesion and Detachment Models Clarkson University

Sphere Attached to a Surface



a = Contact

P = Exerted Force

F_{ad} = Adhesion Force

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Johnson-Kandall-Roberts (1971)

$$a^3 = \frac{d}{2K} \left[P + \frac{3}{2} W_A \pi d + \sqrt{3\pi W_A d P + \left(\frac{3\pi W_A d}{2} \right)^2} \right]$$

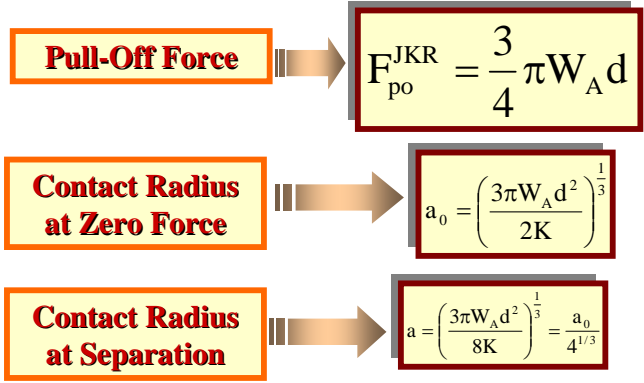
$$K = \frac{4}{3} \left[\frac{1-\nu_1^2}{E_1} + \frac{1-\nu_2^2}{E_2} \right]^{-1}$$

Hertz Model

$$a^3 = \frac{dP}{2K}$$

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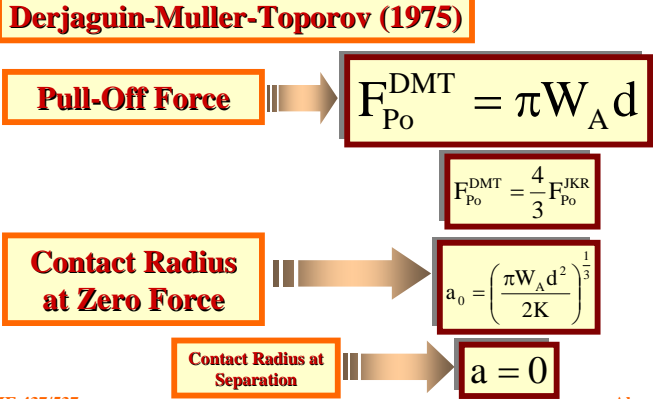
JKR Model Clarkson University



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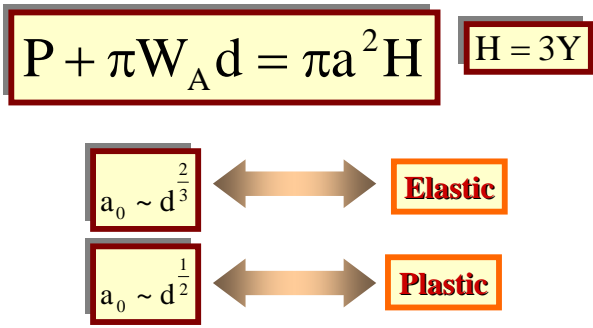
DMT Model Clarkson University



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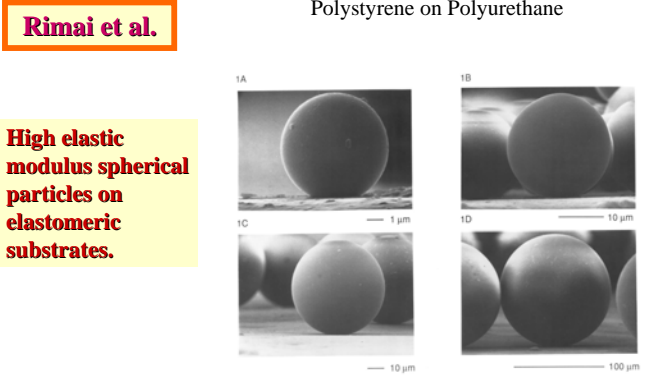
Maugis-Pollock Model Clarkson University



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Examples of Adhesion-Induced Deformations - JKR Systems Clarkson University



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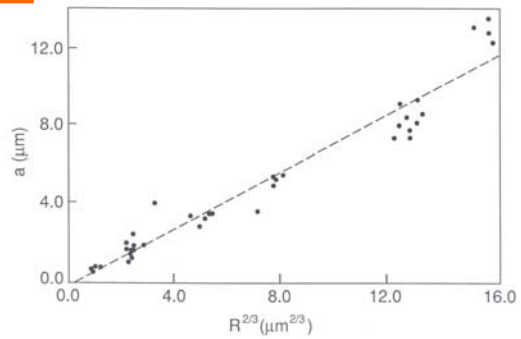
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Examples of Adhesion-Induced Deformations - JKR Systems

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Rimai et al.

GLASS BEADS ON POLYURETHANE SUBSTRATE



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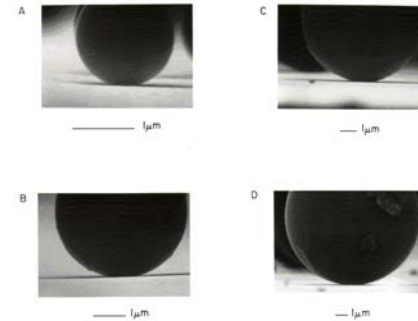
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Non-JKR Systems

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Rimai et al.

Polystyrene particles on a silicon wafer



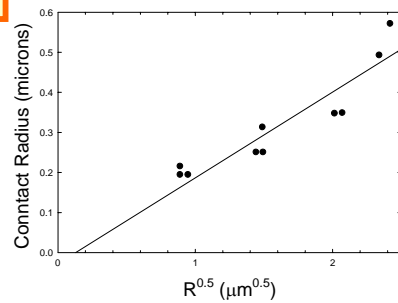
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Non-JKR Systems

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Thermodynamic Work of Adhesion

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$$W_A = \frac{A}{12\pi z_0^2}$$

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JKR Model Clarkson University

$$a^{*3} = 1 - P^* + \sqrt{1 - 2P^*}$$

$$P^* = -\frac{P}{\frac{3}{2}\pi W_A d}$$

$$a^* = \frac{a}{\left(\frac{3\pi W_A d^2}{4K}\right)^{1/3}}$$

$a_0^* = 1.26$

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JKR Model Clarkson University

$$M^{*JKR} = P^* a^* = P^* (1 - P^* + \sqrt{1 - 2P^*})^{1/3}$$

Maximum Moment

→

$M_{\max}^{*JKR} = 0.42$

$$P_{\max}^* = F_{po}^{*JKR} = \frac{F^{*JKR}}{\frac{3}{2}\pi W_A d} = 0.5$$

→

$M^{*JKR} = 0.397$

$P_{\max}^* a_0^* = 0.63$

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DMT Model Clarkson University

Contact Radius

→

$a^3 \approx \frac{d}{2K} (P + \pi W_A d)$

Nondimensional Contact Radius

→

$a^{*3} = \left(\frac{a}{\frac{3\pi W_A d^2}{4K}}\right)^3 = -P^* + \frac{2}{3}$

Resistance Moment

→

$M^{*DMT} = P^* (2/3 - P^*)^{1/3}$

Maximum Moment

→

$M_{\max}^{*DMT} = 0.28$

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JKR-DMT Models Clarkson University

$P_{\max}^* = F_{po}^{*DMT} = \frac{F^{*DMT}}{\frac{3}{2}\pi W_A d} = \frac{2}{3}$

$P_{\max}^* a_0^* = 0.58$

$M^{*DMT} = 0$

Maximum Moments

→

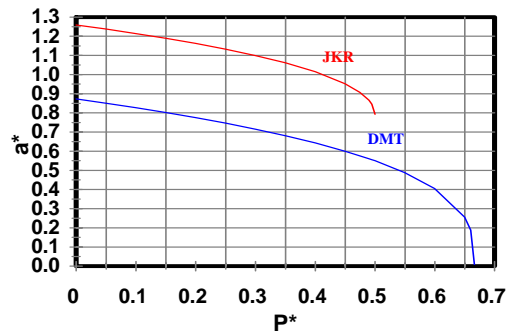
$M_{\max}^{*JKR} = 0.42 = 1.5 M_{\max}^{*DMT}$

$$M_{\max}^{*JKR} = 2.63 \frac{W_A^{4/3} d^{5/3}}{K^{1/3}}$$

$$M_{\max}^{*DMT} = 1.83 \frac{W_A^{4/3} d^{5/3}}{K^{1/3}}$$

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JKR-DMT Models Clarkson University

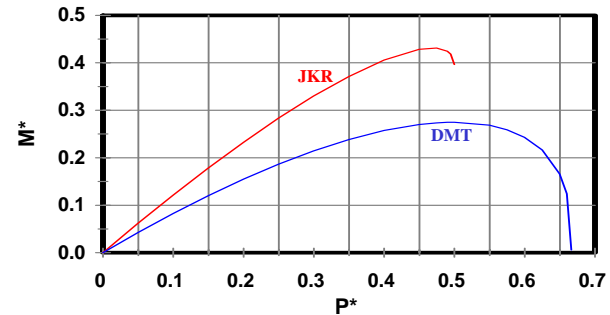


Variations of contact radius with the exerted force.

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JKR-DMT Models Clarkson University



Variations of resistance moment with the exerted force.

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Conclusions Clarkson University

- Spherical particles are removed by overcoming the adhesion rolling resistance
- JKR, DMT and Maugis-Pollock Models
- Contact radius varies differently with d for elastic and plastic deformations

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Thank you!

Questions?

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